

MATHEMATICS

Series B

The answers must be justified.

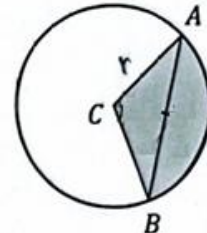
Problem 1 2.0 points

Consider a circle with center C and radius 8 cm.

The area of the gray sector is equal to 15% of the area of the whole disc.

The drawing is not to scale.

Calculate the length of the segment AB .



Problem 2 1.5 points

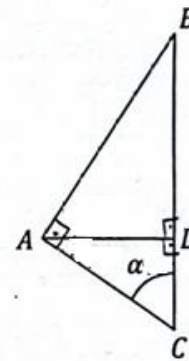
The triangle ABC is a right triangle with right angle at vertex A .

The segment AD is perpendicular to the segment BC .

The length of AD is 20 cm and $\alpha = 50^\circ$.

The drawing is not to scale.

Calculate the area of triangle ABC .



Problem 3 4.0 points

- Calculate all the values of x , $-\pi \leq x \leq \pi$ radians, such that $15 \cos(x) - 4 \sin(x) = 0$.
- Calculate all the values of x , $0 \leq x \leq 2\pi$ radians, such that $10 \cos^2(x) + 2 \sin(x) = 2$.

Problem 4 2.5 points

A part of the graph of $y = 4 \cos(\omega x)$ is given. The point $M(5; -4)$ is a minimum.

Calculate the exact x -coordinates of $P(\dots; 0)$ and $R(\dots; 2)$.

Give the answers as fractions.

