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Name: \_\_\_\_\_

INDICATE YOUR COMPUTATIONS - SIMPLIFY YOUR ANSWERS AS MUCH AS POSSIBLE

**Exercise 1.** / 7 15'

- The sides of a triangle are  $a = 12$ ,  $b = 9$ ,  $c = 5$ . Determine the measures of its three angles.
- The area of a triangle is 100. We know the sides  $a = 20$  and  $b = 15$ . Calculate the possible values for the angle  $\gamma$ .

**Exercise 2.** / 14 25'

Solve the following trigonometric equations.

- $\sin(3x) + 4\cos(3x) = 0$
- $\cos^2(x) + 2\sin(x) = -1$
- $\sin(4x + 20^\circ) = -\sin(2x)$
- $2\arccos(x) = \arctan(1)$

**Exercise 3.** / 5 10'

We give  $\sin(x) = -0.8$  with  $P_x$  in  $Q_{III}$ , and  $\cos(y) = 0.8$  with  $P_y$  in  $Q_{IV}$ .

Determine the value of  $\cos(x - y)$ .

*You're not allowed to use the measures of the angles  $x$  and  $y$ .*

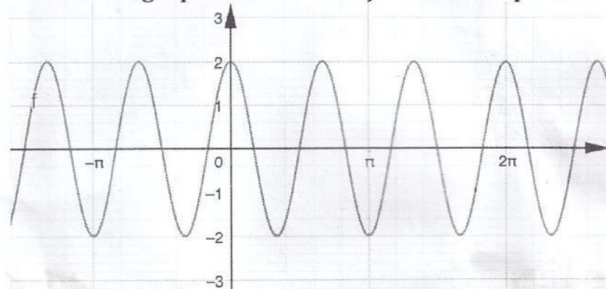
*Justify your answers with computations.*

**Exercise 4.** / 20'

- Give the polar coordinates of the point  $A(-5; 12)$ .
- Determine the Cartesian and polar coordinates of the point  $A'$  that is the reflection of point  $A$  about the  $x$ -axis.
- Point  $A$  is rotated by  $-40^\circ$  about the origin. At what distance from the  $y$ -axis is the point now?
- Give the equation of the steeper line that passes through the point  $(2; 1)$  and forms an angle of  $20^\circ$  with the line  $y = x$ .

**Exercise 5.** / 10 15'

- Give the domain of  $f(x) = \tan(2x)$  ( $x$  is in rad)
- Here is the graph of a function  $f$ . Give its expression.



- Give a function whose period is  $T = 2$ .
- Give the period of  $f(x) = \sin\left(\frac{x}{5}\right) + \tan\left(\frac{x}{4}\right)$  with justifications.
- Give the range of  $f(x) = 5\sin(4x + 3) - 2$