CALCULUS 03.11.2021

- 1) Fill the "definition" of the derivative : $f'(x) = \lim_{x \to a} f'(x) = \lim_{x \to a} f$
- 2) Compute an estimation of the slope of the tangent to the curve $y = \sqrt{2x 1}$ at the point with abscissa 5. Indicate the computations.

3)
$$(-3x + 6)' =$$

$$(x^3 - 2x^2)' =$$

$$(x^5 + 7x^3 - x + 4)' =$$

- 4) Give the equation of the slant asymptotes of $f(x) = \sqrt{4x^2 18x + 8}$
- 5) Give the equation of the asymptotes of $f(x) = x + 2 \sqrt{x^2 + 6}$
- 6) Determine with justifications:

$$\lim_{x\to 0} \frac{x^2 + x}{\sin^2(2x)} =$$

$$\lim_{x\to 0} \frac{\sin(x)}{x^2+1} =$$

$$\lim_{x \to -1} \frac{\sqrt{3-x} - 2}{5x + 5} =$$

Extra questions that do not count for the mark...

Indicate the derivative of $f(x) = x^2 + x$ and use it to give the exact slope of the tangent of the graph of f at the point with abscissa 3.

Give the derivative of $(x) = x^3 - 12x$. Use it to find the coordinates of **one** "vertex" of that curve f.