

EXERCICE 1

$$f_m(x) = (x-m)e^{-x}$$

a) $f_m(x) = 0 \Leftrightarrow x = m$

• $\lim_{x \rightarrow +\infty} \frac{x-m}{e^x} = 0$

$\lim_{x \rightarrow -\infty} \frac{x-m}{e^x} = -\infty$

• $f'(x) = e^{-x} + (x-m)e^{-x} = e^{-x}(1-x+m) = 0 \Leftrightarrow$
 $\Leftrightarrow 1-x+m = 0 \Leftrightarrow x = 1+m$

• $f''(x) = -e^{-x}(1-x+m) + e^{-x}(-1) =$
 $= e^{-x}(-1+x-m-1) = e^{-x}(x-m-2) = 0 \Leftrightarrow$
 $\Leftrightarrow x = m+2$

b) $f_1 = (x-1)e^{-x}$

$f_2(x) = (x-2)e^{-x}$

NOY $f_1(0) = -1$

$f_2(0) = -2$



$$b) f'_u(x) = 0 \Leftrightarrow x = 1+m$$

$$y = (1+m-m)e^{-1-m} = e^{-(1+m)} \Rightarrow \underline{y = e^{-x}}$$

$$d) f_u(m; 0)$$

$$f'_u(m) = 1 \Leftrightarrow e^{-m}(1-m+m) = 1 \Leftrightarrow e^{-m} = 1 \Leftrightarrow e^u = 1$$

$$\Leftrightarrow \underline{m = 0}$$

EXERCICE 2

$$f_1(x) = e^{-x} \quad f_2(x) = e^{-x} \cdot \cos(x)$$

$$a) f_1(x) = f_2(x) \Leftrightarrow e^{-x} = e^{-x} \cos(x) \Leftrightarrow \cos(x) = 1 \Leftrightarrow$$

$$x = 2k\pi \quad k \in \mathbb{Z}$$

$$b) f'_1(x) = -e^{-x} \quad f'_2(x) = -e^{-x} \cos(x) - e^{-x} \sin(x) =$$

$$= -e^{-x} (\cos(x) + \sin(x))$$

$$f'_1(2k\pi) = -e^{-2k\pi}$$

$$f'_2(2k\pi) = -e^{-2k\pi} (\underbrace{\cos 2k\pi}_1 + \underbrace{\sin 2k\pi}_0) = -e^{-2k\pi}$$

Donc $f'_1(2k\pi) = f'_2(2k\pi)$ et

$$f_1(2k\pi) = e^{-2k\pi} = f_2(2k\pi) = e^{-2k\pi} \underbrace{\cos 2k\pi}_1$$

Alors les deux graphes possèdent la même tangente en $x = 2k\pi \quad \forall k \in \mathbb{Z}$
 $\Rightarrow$ ils sont tangents