

LDDR - Niveau 2-TE1: Ensembles

EXERCICE 1

a) $A = \{x \mid x = (-1)^n \frac{(n-2)^2}{2(n+1)} \quad n \leq 4, n \in \mathbb{N}^*\}$

$n=1 \quad x = -\frac{1}{4}$ $n=2 \quad x = 0$
 $n=3 \quad x = -\frac{1}{8}$ $n=4 \quad x = \frac{4}{10} = \frac{2}{5}$

$A = \{-\frac{1}{4}; 0; -\frac{1}{8}; \frac{2}{5}\}$

b) $B = \{x \mid x^2(2x^2+3)(x^2-1) = 0 \quad x \in \mathbb{Z}\}$

$x^2(2x^2+3)(x-1)(x+1) = 0 \Leftrightarrow x=0, x=1, x=-1$

$B = \{0; 1; -1\}$

EXERCICE 2

$E = \{x \mid x = n, n < 13, n \in \mathbb{N}^*\} \quad A = \{1; 2; 3; 4; 5\}$

$\bar{B} = \{4; 7; 11\} \quad E = \{1; 2; \dots; 12\} \quad \bar{A} = \{6; 7; \dots, 12\}$

$B = \{1; 2; 3; 5; 6; 8; 9; 10; 12\}$

$B \cap \bar{A} = \{6; 8; 9; 10; 12\}$

EXERCICE 3

1. $A = [-5, +\infty[$ 

$B =]-7; 3]$ 

$C = [1; 5[$ 

2. $A \cup B =]-7, +\infty[\quad (A \cup B) \setminus C =]-7; 1[\cup [5, +\infty[$

$B \cap C = [1; 3]$ $B \setminus (B \cap C) =]-7; 1[$

EXERCICE 4

a) $(2a+b)(a-b) - (2a+b) = (2a+b)(a-b-1)$

b) $x(a-b) - y(b-a) = x(a-b) + y(a-b) = (a-b)(x+y)$

c) $2k^2 - l^2k + 2k^3 - l^2 = 2k^2(1+k) - l^2(k+1) = (k+1)(2k^2 - l^2) = (k+1)(\sqrt{2}k - l)(\sqrt{2}k + l)$

EXERCICE 5

a) $\frac{x-\sqrt{7}}{x^2-7} = \frac{x-\sqrt{7}}{(x-\sqrt{7})(x+\sqrt{7})} = \frac{1}{x+\sqrt{7}}$

b) $\frac{49x^2 - 28xy + 4y^2}{7x-2y} = \frac{(7x-2y)^2}{7x-2y} = 7x-2y$

$$\begin{aligned}
 c) \quad \frac{81x^3 - 18x^2 + x}{1 - 81x^2} &= \frac{x(81x^2 - 18x + 1)}{(1 - 9x)(1 + 9x)} = \frac{x(9x - 1)^2}{(1 - 9x)(1 + 9x)} \\
 &= \frac{x(9x - 1)}{-(9x + 1)} = \frac{x(1 - 9x)}{9x + 1}
 \end{aligned}$$